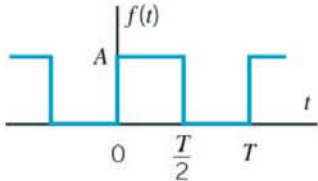
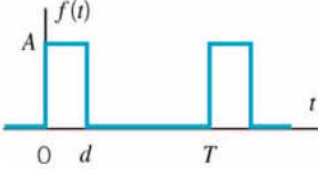
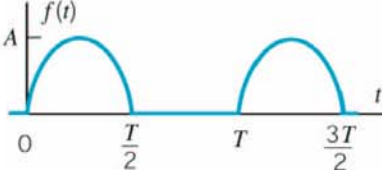
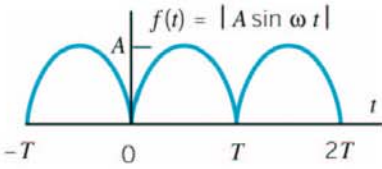
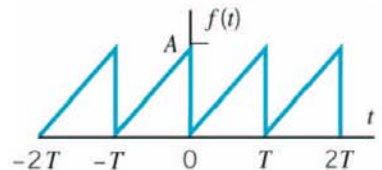
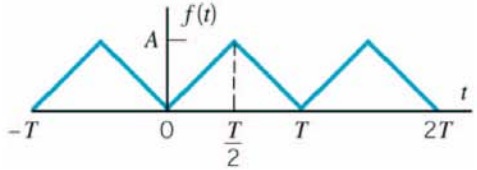


$$\begin{aligned}
 s(t) & : S_n = R_n + jI_n \\
 s(t) \text{ reale} & : S_n = S_{-n}^* \\
 s(t) \text{ pari, } s(t) = s(-t) & : S_n = S_{-n} \\
 s(t) \text{ reale e pari} & : S_n = R_n = R_{-n} \\
 s(t) \text{ dispari, } s(t) = -s(-t) & : S_n = -S_{-n} \\
 s(t) \text{ reale e dispari} & : S_n = jI_n = -jI_{-n} \\
 s(t) \text{ alternativo, } s(t) = -s(t + T_0/2) & : S_{2k} = 0
 \end{aligned}$$

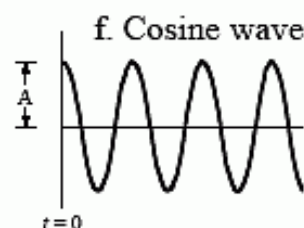
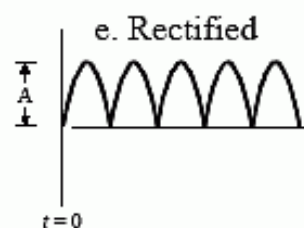
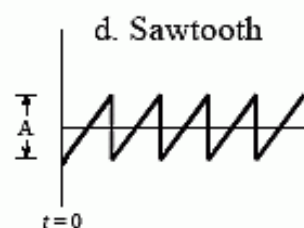
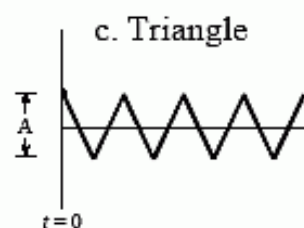
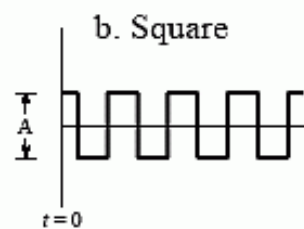
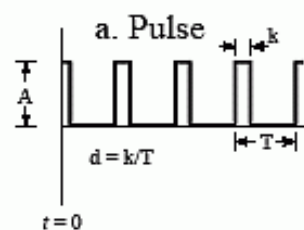
PROPRIETA'	SEGNALE	SF
	segnale continuo periodico, di periodo T_0 , a potenza finita	S_n $f_0 = 1/T_0$
	$s(t) = \sum_{n=-\infty}^{\infty} S_n e^{j2\pi nt/T_0}$	$S_n = \frac{1}{T_0} \int_{t_0}^{t_0+T_0} s(t) e^{-j2\pi nt/T_0} dt$
LINEARITA'	$ax(t) + by(t)$	$aX_n + bY_n$
TRASLAZIONE TEMPORALE	$s(t - t_0)$	$S_n e^{-j2\pi nt_0/T_0}$
TRASLAZIONE IN FREQUENZA	$s(t) e^{j2\pi mt/T_0}$	S_{n-m}
DERIVAZIONE TEMPORALE	$ds(t)/dt$	$(j2\pi n/T_0)S_n$
INTEGRAZIONE	$\int_{-\infty}^t s(\alpha) d\alpha$	$(T_0/j2\pi n)S_n$
INVERSIONE ASSE TEMPI	$s(-t)$	S_{-n}
CONIUGAZIONE	$s^*(t)$	S_{-n}^*
CONVOLUZIONE TEMPORALE	$s(t) = (1/T_0) \int_{t_0}^{t_0+T_0} x(\tau) y(t-\tau) d\tau$	$S_n = X_n Y_n$
PRODOTTO (Convoluzione in frequenza)	$s(t) = x(t) y(t)$	$S_n = \sum_{k=-\infty}^{\infty} X_k Y_{n-k} = (X_n \otimes Y_n)/f_0$
CORRELAZIONE TEMPORALE	$s(t) = (1/T_0) \int_{t_0}^{t_0+T_0} x(\tau) y^*(\tau-t) d\tau$	$S_n = X_n Y_n^*$
CORRELAZIONE IN FREQUENZA	$s(t) = x(t) y^*(t)$	$S_n = \sum_{k=-\infty}^{\infty} X_k Y_{k-n}^* = (X_n \otimes Y_{-n}^*)/f_0$

$$\begin{aligned}
 \frac{1}{T_0} \int_{t_0}^{t_0+T_0} x(\tau) y^*(\tau) d\tau &= \sum_{n=-\infty}^{\infty} X_n Y_n^* \\
 \frac{1}{T_0} \int_{t_0}^{t_0+T_0} |x(t)|^2 dt &= \sum_{n=-\infty}^{\infty} |X_n|^2
 \end{aligned}$$

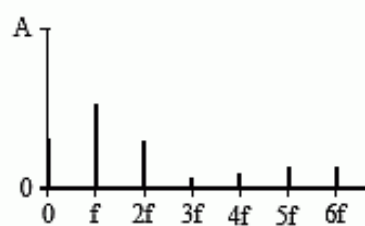
Table 15.4-1 The Fourier Series of Selected Waveforms.

Function	Trigonometric Fourier Series
	<p>Square wave: $\omega_0 = \frac{2\pi}{T}$</p> $f(t) = \frac{A}{2} + \frac{4A}{\pi} \sum_{n=1}^{\infty} \frac{\sin((2n-1)\omega_0 t)}{2n-1}$
	<p>Pulse wave: $\omega_0 = \frac{2\pi}{T}$</p> $f(t) = \frac{Ad}{2} + \frac{2Ad}{\pi} \sum_{n=1}^{\infty} \frac{\sin\left(\frac{n\pi d}{T}\right)}{\frac{n\pi d}{T}} \cos(n\omega_0 t)$
	<p>Half wave rectified sine wave: $\omega_0 = \frac{2\pi}{T}$</p> $f(t) = \frac{A}{\pi} + \frac{A}{2} \sin \omega_0 t - \frac{2A}{\pi} \sum_{n=1}^{\infty} \frac{\cos(2n\omega_0 t)}{4n^2 - 1}$
	<p>Full wave rectified sine wave: $\omega_0 = \frac{2\pi}{T}$</p> $f(t) = \frac{2A}{\pi} - \frac{4A}{\pi} \sum_{n=1}^{\infty} \frac{\cos(n\omega_0 t)}{4n^2 - 1}$
	<p>Sawtooth wave: $\omega_0 = \frac{2\pi}{T}$</p> $f(t) = \frac{A}{2} + \frac{A}{\pi} \sum_{n=1}^{\infty} \frac{\sin(n\omega_0 t)}{n}$
	<p>Triangle wave: $\omega_0 = \frac{2\pi}{T}$</p> $f(t) = \frac{A}{2} - \frac{4A}{\pi^2} \sum_{n=1}^{\infty} \frac{\cos((2n-1)\omega_0 t)}{(2n-1)^2}$

Time Domain



Frequency Domain

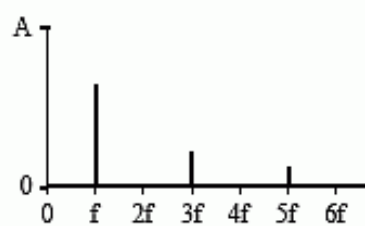


$$a_0 = A d$$

$$a_n = \frac{2A}{n\pi} \sin(n\pi d)$$

$$b_n = 0$$

($d = 0.27$ in this example)

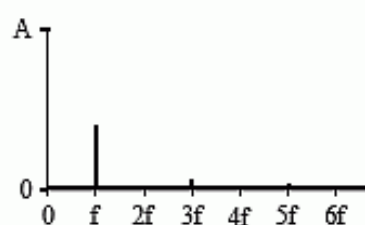


$$a_0 = 0$$

$$a_n = \frac{2A}{n\pi} \sin\left(\frac{n\pi}{2}\right)$$

$$b_n = 0$$

(all even harmonics are zero)

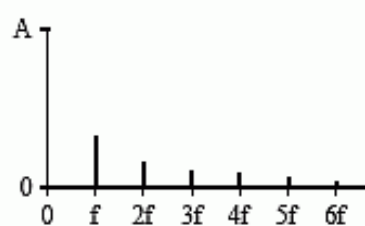


$$a_0 = 0$$

$$a_n = \frac{4A}{(n\pi)^2}$$

$$b_n = 0$$

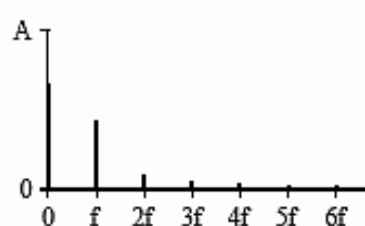
(all even harmonics are zero)



$$a_0 = 0$$

$$a_n = 0$$

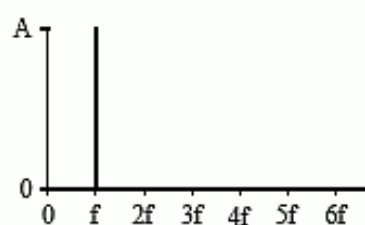
$$b_n = \frac{A}{n\pi}$$



$$a_0 = 2A/\pi$$

$$a_n = \frac{-4A}{\pi(4n^2 - 1)}$$

$$b_n = 0$$



$$a_1 = A$$

(all other coefficients are zero)

FIGURE 13-10

Examples of the Fourier series. Six common time domain waveforms are shown, along with the equations to calculate their "a" and "b" coefficients.